
Paradox

Issue 3, 2005

THE MAGAZINE OF THE MELBOURNE UNIVERSITY MATHEMATICS AND STATISTICS SOCIETY



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PRINTED:	October, 2005

Words From the Editor

Paradox has a long history of encouraging and documenting mathematical super heroes of all descriptions. We are there when they are born (even if it's through the fourth dimension), when they hone their powers, we are there egging them on to perform ridiculous feats of alcohol- and caffeine-fuelled mathematical daring at their 21st parties, and we are there, wiping away a tear, when they vanquish their first evil economic rationalist university administrator or crazed physicist. In this edition, the last of 2005, the full exploits of Paradox Kid and Knot Man are related in full.

Paradox Kid first appeared in Paradox in 1999, and continued until 2001. It was written by Jeremy Glick and Sally Miller. Dan Mathews and Priscilla Brown took the baton in 2002 and started to write/draw Knot Man. We hope you enjoy this collection of their finest work.

— Nick Sheridan

Preface to a Compendium of Mathematical Superheroism

In the beginning was mathematics. Mathematics may precede us, but is revealed to us by the great. As long as there has been mathematics with us, there have been the great. Greatness produces mathematics; mathematics produces greatness; mathematics is greatness. And the mathematical superhero personifies the zenith of this greatness. Who are they? Where do they come from? What is their purpose? What do they do? Why? And why do they all have such bad fashion sense?

They were not called upon. They were not crowned in glory. They were not elected, selected, or appointed to the job. They were not born with a silver spoon; even though some were born through the fourth dimension. Some were discreet; but others were continuous. Some were straightlaced; but others are a little more knotty.

For the mathematical superhero is a complex character.¹ The mathematical superhero is a function of many variables.² The mathematical superhero is just one element in a free associative group.³ The mathematical superhero knows no boundaries⁴ — something of a closed manifold.⁵ The mathematical

¹ *Complex*? Get it? 5 points for appreciating the mathematical pun. *Character*? Get it? 30 points for this one.

² 10 points.

³ 15 points.

⁴ 10 points.

⁵ 40 points.

superhero, in the end, though there are variations,⁶ solves the problem, and with minimal energy⁷ — something of a geodesic.⁸ He or she may be rather twisted,⁹ may be rather tangled,¹⁰ but transforms well under change of variables¹¹ — something of a tensor, really.¹² The mathematical superhero comes in many varieties¹³ — is often stalked¹⁴ — but is always enough to foil any evil scheme¹⁵ from any point in the spectrum,¹⁶ from the most generic¹⁷ to the most maximal.¹⁸ No, greatness was thrust upon them. Their geekiness knew no bounds, and they revelled in things other than sport. Their intellects overtook them, and could only express itself in strange and bizarre outgrowths: spiky-haired protrusions, strange capes and outrageous socks and sandals. And in matters linguistic, a tendency — or rather, an irresistible compulsion — to pun relentlessly and atrociously on mathematical terms, well beyond any reasonable limit.¹⁹ They could not help themselves; they could not avoid it; that would be an infinite descent.²⁰ Powered with coffee — the product of the cup²¹ — more bad mathematical puns have been made than was ever thought possible, and mathematical harmony has been restored to the universe time and time again.

For not everyone can be a mathematical superhero. Not everyone can make terrible mathematical puns as consistently and as appallingly. Not everyone can save the world from a maniacal physicist/economist/vice-chancellor/(insert your least favourite non-mathematical person here) with an evil and suitably twisted and ridiculous plan to take over the world — or, much the same thing, the mathematics department. Not everyone can be so utterly inept at every facet of human endeavour other than world-saving heroism. Not everyone refers to a donut as ‘genus-1 nutrition’. And not everyone is so comfortable with Cauchy’s formulation of continuity as to be named after its essential variables. Yes, the world needs mathemagicians to look up to. Yes, even if they arise from the demented vision of a twisted author in the rather obscure genre of

⁶20 points.

⁷20 points.

⁸Bonus 50 points for your knowledge of differential geometry!

⁹10 points.

¹⁰30 points.

¹¹10 points.

¹²50 points.

¹³30 points.

¹⁴40 points.

¹⁵30 points — bonus 50 points if you know the definition of a scheme!

¹⁶Minus 200 points for knowing way too much algebraic geometry!

¹⁷Minus 500 points more, this is getting ridiculous.

¹⁸Minus 50 points.

¹⁹Oh yes, beyond any reasonable limit: 20 points.

²⁰20 points.

²¹50 points. (No, not for ‘product’, but for ‘cup product’.)

mathematical comics.

But we should not go too far. We should not put these heroes on a pedestal. For in a sense, the mathematical superhero is everywoman and everyman. Is there not really, deep in our hearts, a mathematical superhero in all of us? We need to unlock our potential, remove our cutoff functions, and drink too much coffee. We must disgorge ourselves of all selfishness, avarice, and fashion sense. We must rail against injustice, iniquity, and inelegance. We must take action, when necessary, and apply our knowledge to the real world, sometimes, when we really have to, and physicists or engineers will not do it for us. In this humble collection, you will see some of the finest examples of mathematical superheroes ever produced. You will be taken to heights of superhero magnificence greater than N , for any given $N > 0$. So let us proceed.

— Daniel Mathews, 8/10/05, Stanford, USA

Results

- 400+: You are truly one of the great. You have *more brains than the basket behind a guillotine*, and *more sexual allure than a hyperbolic attractor*.
- 300–400: You are almost there. Try wearing socks and sandals more often. You might even like to get yourself a cape or a *supervisor*.
- 200–300: You are well on your way. You should read more comics about the exploits of mathematical superheroes. Lucky, then, that you are reading this. But please refrain from battling any but the most minor villains. You will need yet to obtain *more power than a quintic (5)*.
- 100–200: Above average. You have potential, but you have much to learn in our ways. Yes, there is a mathematical superhero inside you. But you will need to obtain a *transcendental extension in all fields* first.
- 50–100: You have yet to make an impression in the world of mathematical superheroism, but yet you can succeed. You have made a start, but there is a long way to go. Your first task is to become *more caffeinated than a convoy of long-haul truck drivers* and *more poised than a stable 2-cycle*.
- 0–50: Perhaps you would be better leaving the crazed physicists and economists and vice-chancellors to others.
- Less than 0: You know way too much algebraic geometry. *Shame on you!*

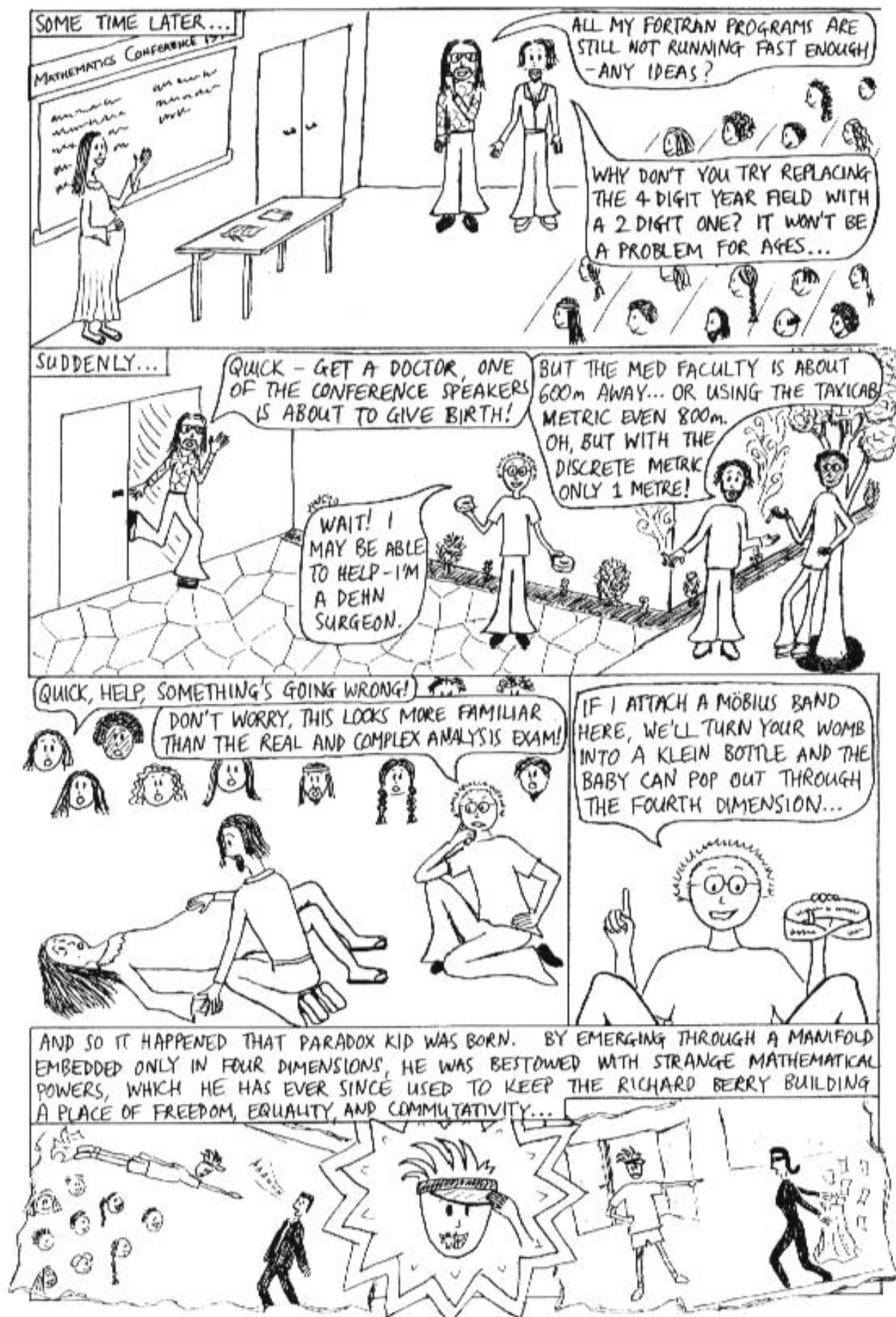














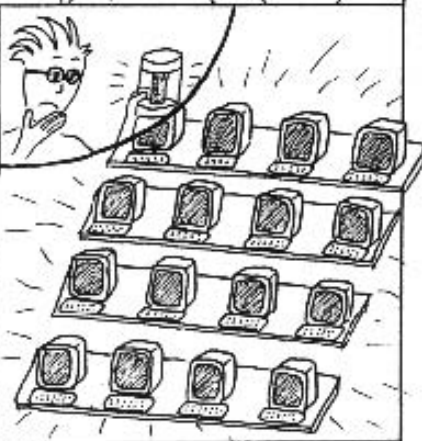


MULDER AND SCULLY! WHAT ARE YOU DOING HERE?
 OUR SCANNERS PICKED UP AN ENORMOUS AMOUNT OF GAMMA RADIATION COMING FROM THIS ROOM.
 WE ASSUMED ALIENS HAD LANDED.
 APPARENTLY IT'S JUST THESE iMACS.
 WHAT CAN WE DO? LAB ATTENDANCE IS LOWER THAN ANY GIVEN $E > 0$.
 MAYBE YOU CAN USE THESE GAMMA RADIATION ABSORBERS THAT WE FOUND IN AN INCA PYRAMID LAST WEEK...



... JUST PUT SEVEN OF THESE ABSORBERS ON TOP OF SEVEN OF THE iMAC MONITORS.

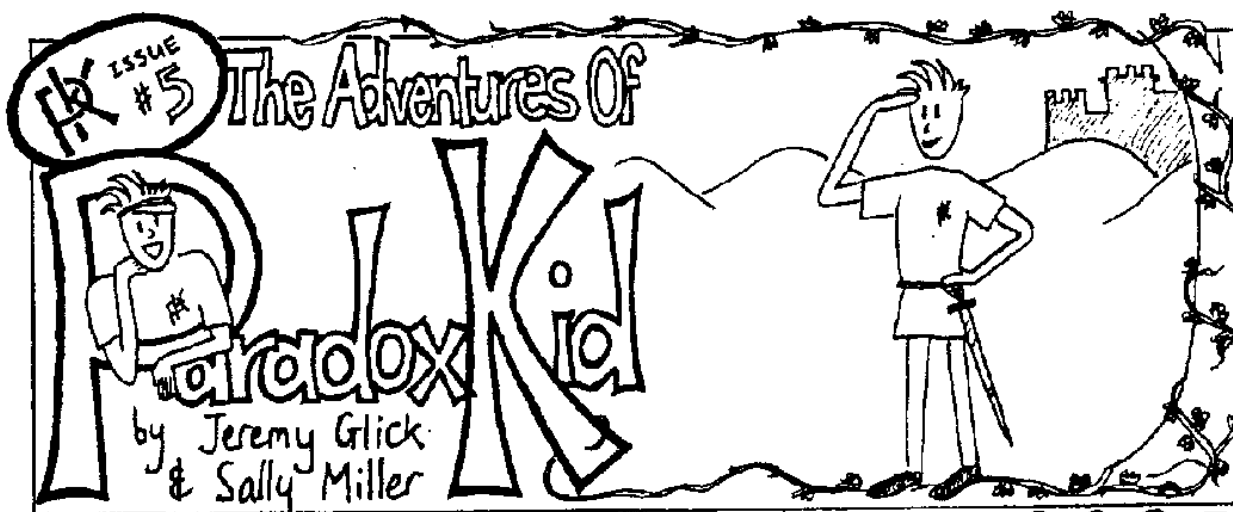
BUT REMEMBER, IF TWO ROWS AND TWO COLUMNS OF iMACS CONTAIN ALL THE ABSORBERS THEN YOU'LL USHER IN AN AGE OF DARKNESS, TERROR, AND PROOFS LEFT TO THE READER.



★ CAN YOU HELP P.K. PLACE THE SEVEN GAMMA RADIATION ABSORBERS ON TOP OF THE iMAC MONITORS (A 4×4 GRID) SO THAT NO TWO ROWS AND TWO COLUMNS CONTAIN ALL THE ABSORBERS?

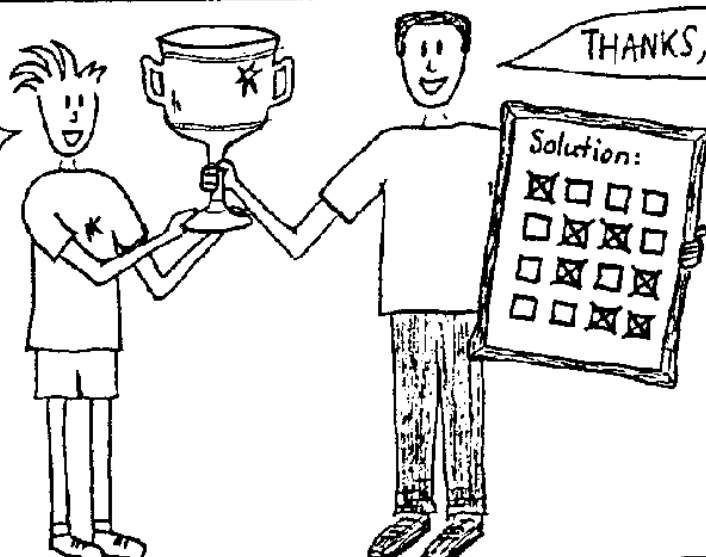
★ THE PERSON WHO SUBMITS THE BEST ANSWER TO THE M.U.S. PIGEONHOLE (NEAR THE MATHS & STATS OFFICE) WILL WIN A CAMEO APPEARANCE IN THE NEXT EDITION OF PARADOX KID!

★ BONUS: PROVE THAT WITH LESS THAN SEVEN GAMMA RADIATION ABSORBERS PLACED ON A 4×4 GRID ONE CAN ALWAYS PICK TWO ROWS AND TWO COLUMNS THAT CONTAIN THEM ALL.



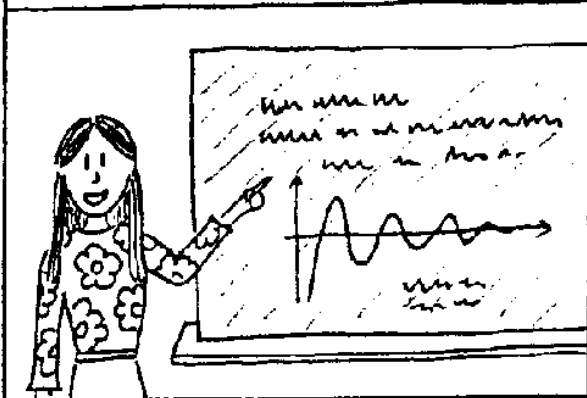
TWO FIELDS, BOTH ALIKE IN OBSCURITY,
 IN FAIR MATHS AND STATS WHERE WE LAY OUR SCENE,
 FROM ANCIENT GRUDGE BREAK TO NEW MUTINY,
 WHERE ADMINISTRATIVE BLOOD MAKES ADMINISTRATIVE HANDS UNCLEAN.
 FROM FORTH THE FATAL RESEARCH OF THESE TWO FOES,
 A PAIR OF DOT-CROSS'D MATHEMATICIANS TAKE THEIR CAREER,
 WHOLE MISADVENTURED PITEOUS OVERTHROWS,
 DO WITH THEIR FATE BURY THEIR RESEARCH GROUPS' STRIFE...

OH, BUT BEFORE
 WE GET INTO THE
 STORY, WE HAVE TO
 AWARD A PRIZE TO
 ANDREW ROGERS
 FOR SOLVING
 LAST ISSUE'S
 PROBLEM!

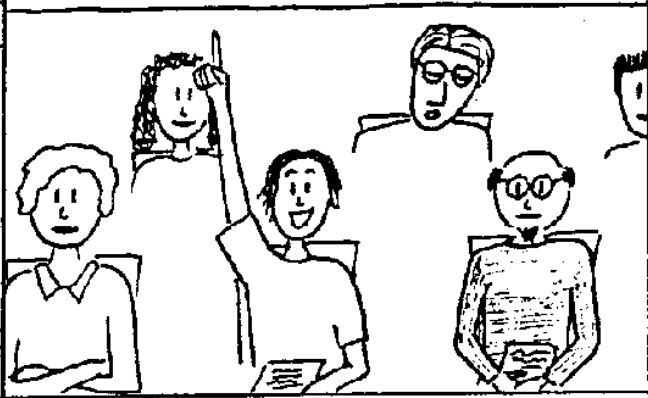


ANYWAY, THIS IS THE STORY OF ρ -MED (RHO-MED) AND JULIASET, TWO OF THE TOP YOUNG RESEARCHERS OF THIS DEPARTMENT. ρ -MED WAS A NEW HONOURS STUDENT IN THE PURE MATHS RESEARCH GROUP. JULIASET WAS A YOUNG LECTURER IN APPLIED. FOR YEARS THE TWO RESEARCH GROUPS HAD HATED EACH OTHER, AND PEOPLE FROM ONE GROUP WERE FORBIDDEN TO WRITE PAPERS WITH PEOPLE FROM THE OTHER...

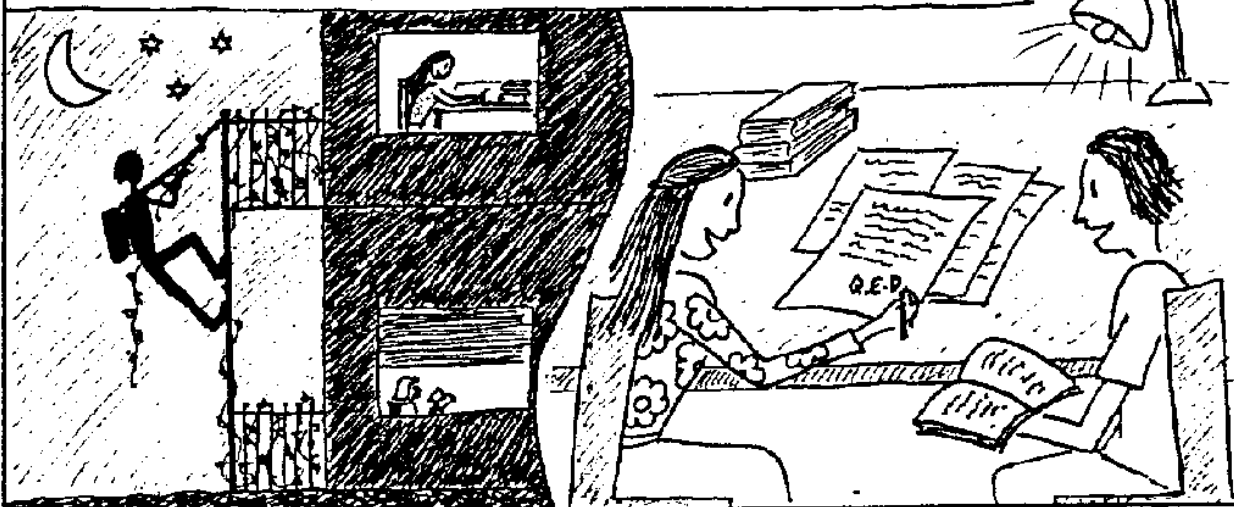
... ONE DAY p-MEO, DESPITE ALL HIS GROUP'S WARNINGS TO THE CONTRARY, ATTENDED A SEMINAR GIVEN BY THE APPLIED GROUP. JULIASET WAS GIVING THE SEMINAR THAT DAY.



HE FELL IN LOVE WITH HER RESEARCH, AND AS SOON AS HE ASKED A QUESTION AFTER HER TALK, SHE FELL IN LOVE WITH HIS MATHEMATICAL INTELLECT TOO. THEY KNEW THEY'D HAVE TO WORK TOGETHER.



SO, MANY EVENINGS p-MEO WOULD CLIMB INTO JULIASET'S OFFICE VIA THE BALCONY AND THEY WOULD RESEARCH TILL DAWN.



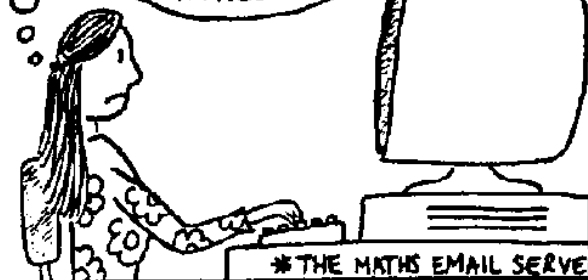
THE TIME WAS APPROACHING WHEN p-MEO WOULD HAVE TO CHOOSE A SUPERVISOR. HE DESPERATELY WANTED TO BE SUPERVISED BY JULIASET, BUT HIS GROUP WOULDN'T HEAR OF IT.



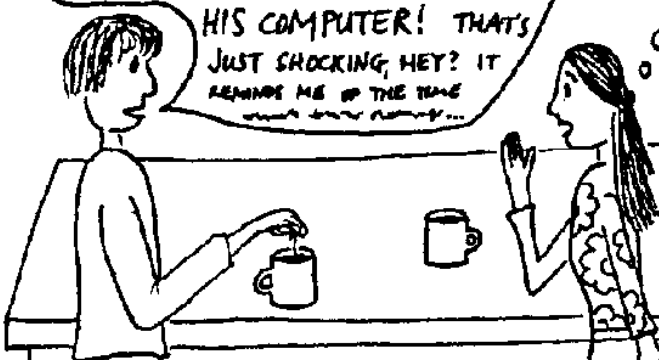


SO ALL WAS GOING TO PLAN: THE PURE STAFF NO LONGER THOUGHT ABOUT COERCING P-MEO TO STAY IN THEIR GROUP, AND JULIASET HAD ONLY TO READ HER EMAIL AND THEN WAIT FOR THE 30 DAY EVALUATION PERIOD TO BE OVER BEFORE SHE COULD BEGIN TO RESEARCH WITH HER YOUNG PROTÉGÉ. UNFORTUNATELY...

OH BUMMER, TINCAN* IS DOWN AGAIN. I GUESS I WON'T BE ABLE TO CHECK MY EMAILS FOR A WHILE...



HEY JULIASET, DID YOU HEAR? P-MEO INSTALLED TETRIS ON HIS COMPUTER! THAT'S JUST SHOCKING, HEY? IT REMINDS ME OF THE TIME



OH NO, POOR P-MEO! WHAT HAS HE DONE?! HOW CAN I EVER WORK AGAIN KNOWING THAT HE GAVE UP HIS CAREER RATHER THAN WORK WITH SOMEONE OTHER THAN ME... I'M GOING TO INSTALL TETRIS TOO!

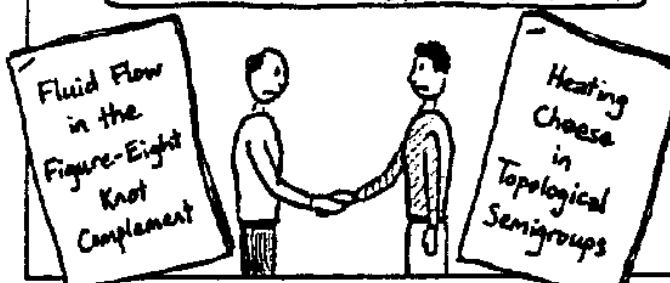
30 DAYS LATER P-MEO EMERGES FROM HIS TETRIS-INDUCED DAZE. HE RUNS STRAIGHT TO JULIASET'S OFFICE TO COLLABORATE, BUT...



...AND SO P-MEO INSTALLED THE FULL VERSION OF TETRIS ON HIS COMPUTER TOO, AND THE MELBOURNE UNI MATHS AND STATS DEPARTMENT LOST TWO OF ITS FINEST YOUNG RESEARCHERS.



SEEING THEIR LOSS, THE TWO RESEARCH GROUPS ENDED THEIR FEUD AND PUBLISHED MANY FINE PAPERS TOGETHER.



SO REMEMBER, DESPITE WHAT WE LEARN FROM SET THEORY, THE WHOLE IS GREATER THAN THE SUM OF THE PARTS. SO COLLABORATE FREELY AND FORM UNIONS WITH PEOPLE EVEN IF YOUR FIELDS ARE DISJOINT. FINALLY, STAY AWAY FROM TETRIS BEFORE YOUR UPCOMING EXAMS!



THE END

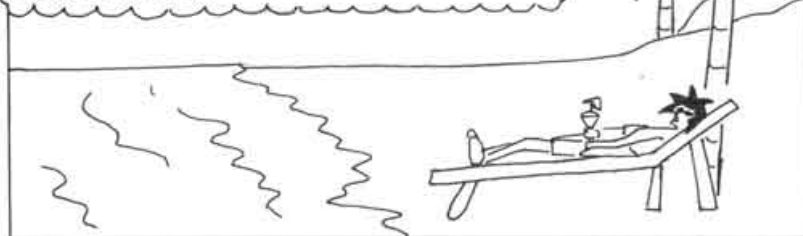








AFTER HIS LATEST BOUT OF SAVING THE UNIVERSE, THEODORE J. KNOTT HAS DECIDED TO TAKE SOME TIME OUT TO RECUPERATE, ON A TROPICAL ISLAND PARADISE...



... WHERE IT SO HAPPENS THAT ONE-TIME SUPERHERO AND MATHEMAGICIAN **PARADOX KID** IS ENJOYING HIS RETIREMENT.



PK, I LOVED YOUR WORK! IT'S BECAUSE OF YOU THAT THE MATHS DEPARTMENT IS SUCH A FREE ASSOCIATIVE GROUP!

OH, THANKS THEODORE J.! LET'S GO GET SOME SNACKS OF THE GENUS-1 MATHS VARIETY!

SO THEODORE J. AND PK, AFTER A HEARTY DOSE OF GENUS-1 DONUTS, REGALED EACH OTHER OF THEIR RESPECTIVE ADVENTURES.



BUT THEODORE J. KNOTT HAD SOMETHING TO ASK OF THE LEGENDARY PK...

... SO NOW, LIFE IS AS SMOOTH AS A **RIEMANNIAN MANIFOLD**!



I WANT TO LEARN MORE IN THE WAYS OF DEFENDING THE MATHEMATICAL UNIVERSE! CAN YOU HELP ME?

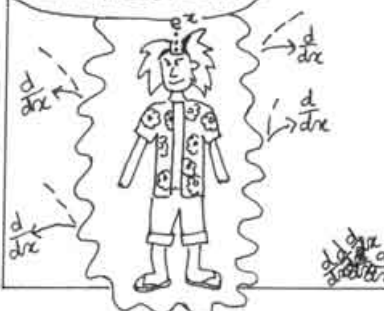
BY GÖDEL, IT'S BEEN LONGER THAN THE PROOF OF FERMAT'S LAST THEOREM, BUT I'LL GIVE IT A TRY!

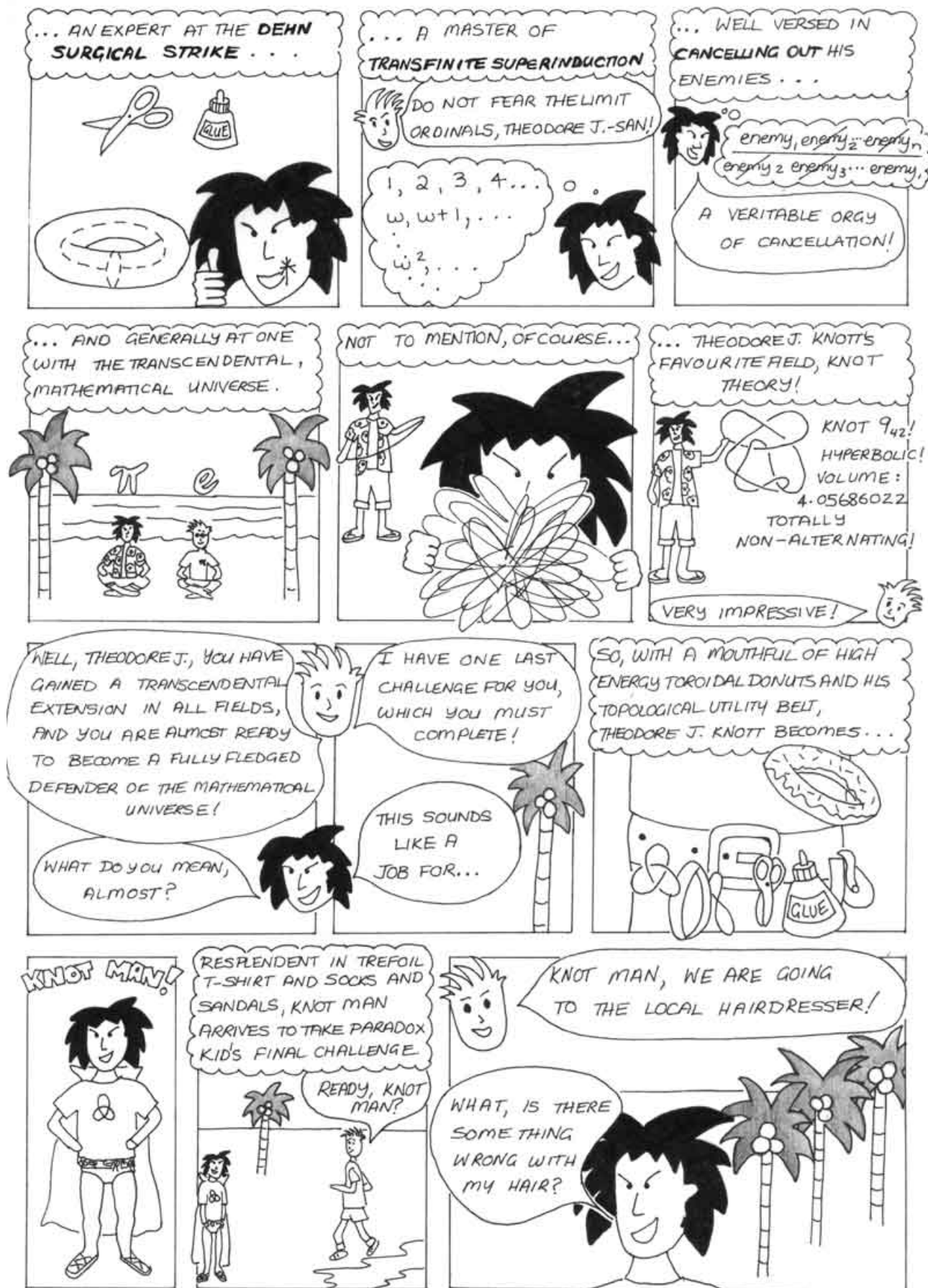
THE GREAT PK THUS TOOK THEODORE J. KNOTT UNDER HIS TUTORAGE...

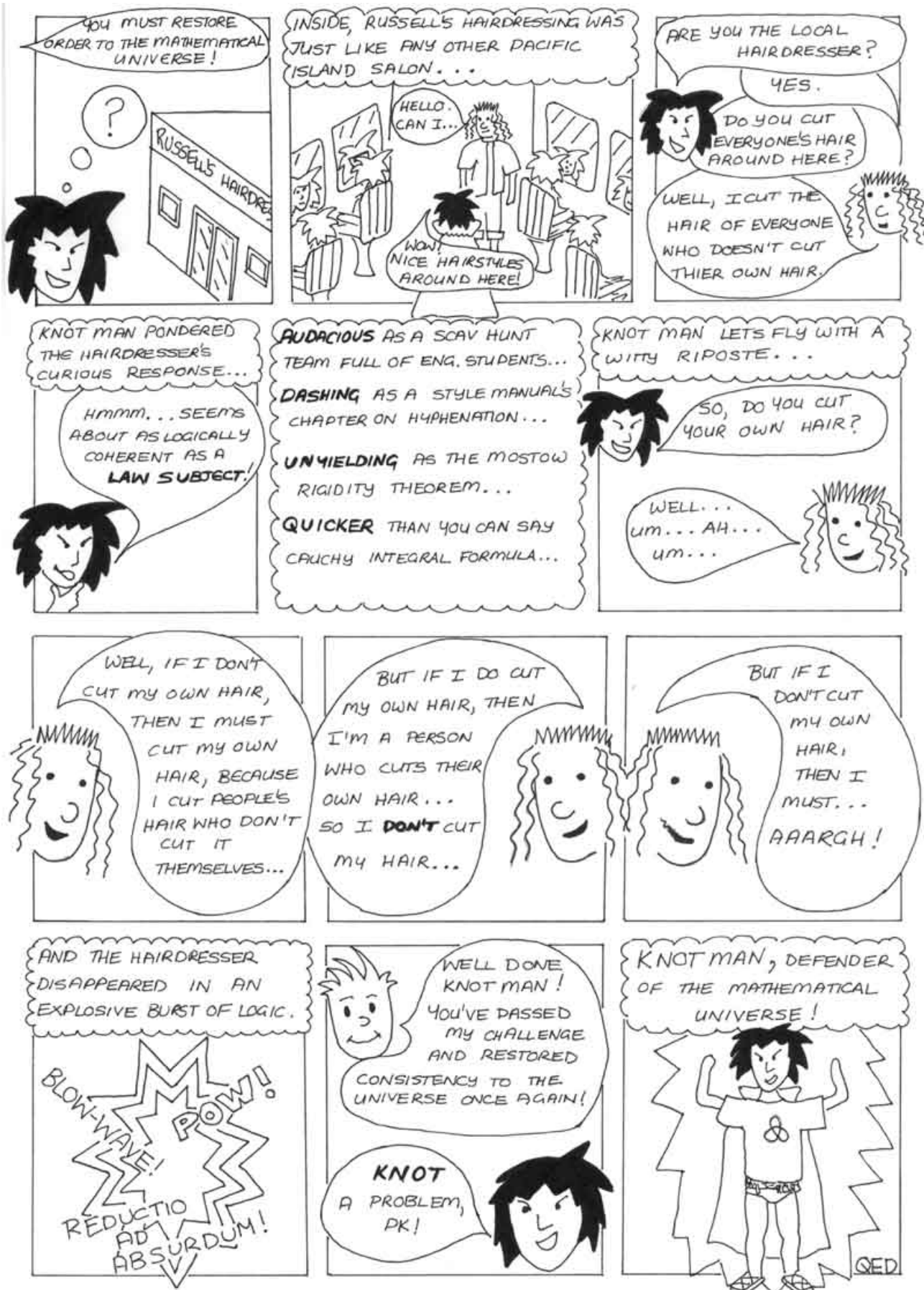
THEODORE J. KNOTT, I WILL SHOW YOU HOW TO OBTAIN
MORE POWER THAN A QUINTIC(5)
MORE BRAINS THAN THE BASKET BEHIND A GUILLOTINE, AND
MORE SEXUAL ALLURE THAN A HYPERBOLIC ATTRACTOR!

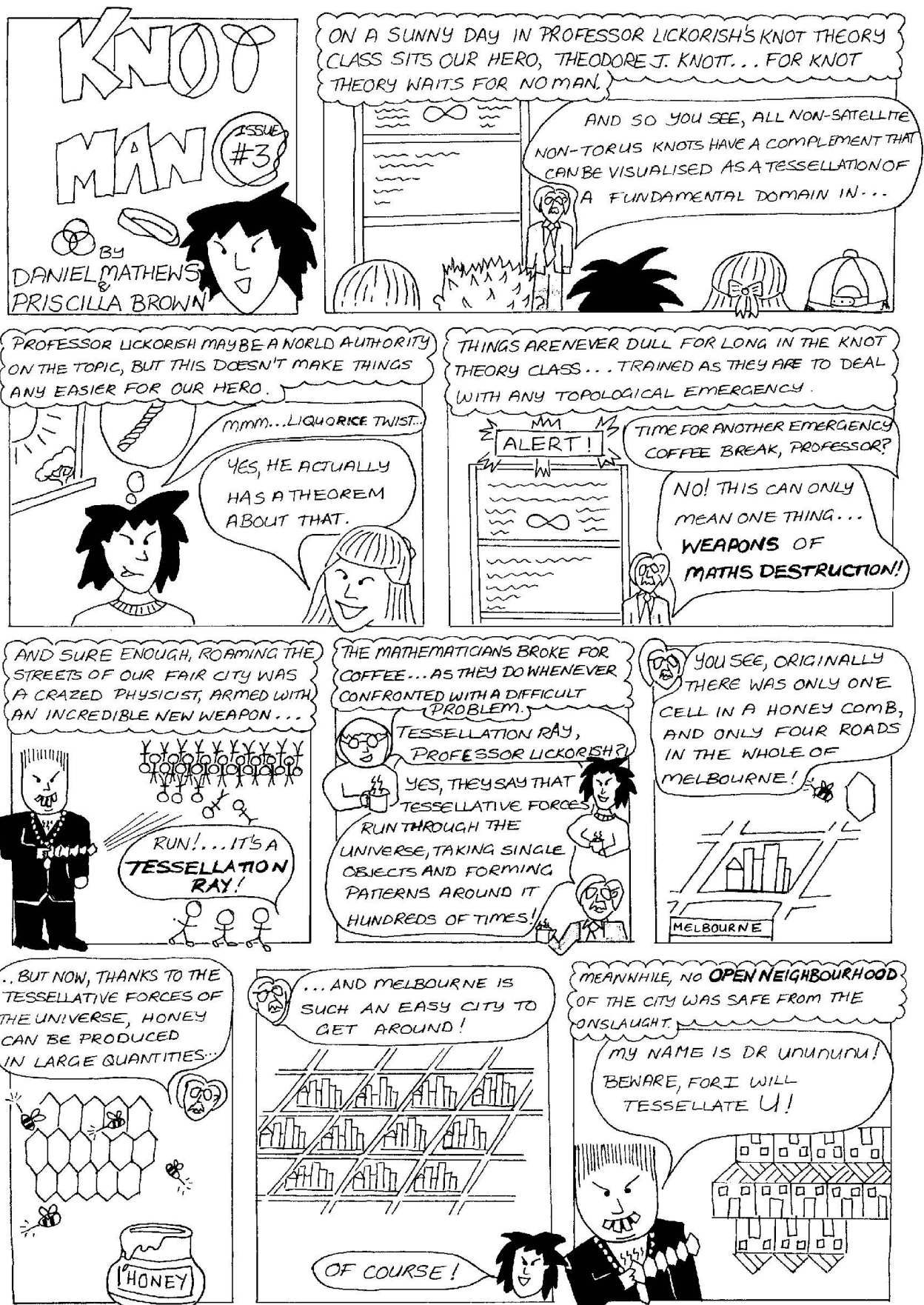
PK TAUGHT THEODORE J. TO BECOME INVULNERABLE TO ALL **DIFFERENTIAL ATTACKS...**

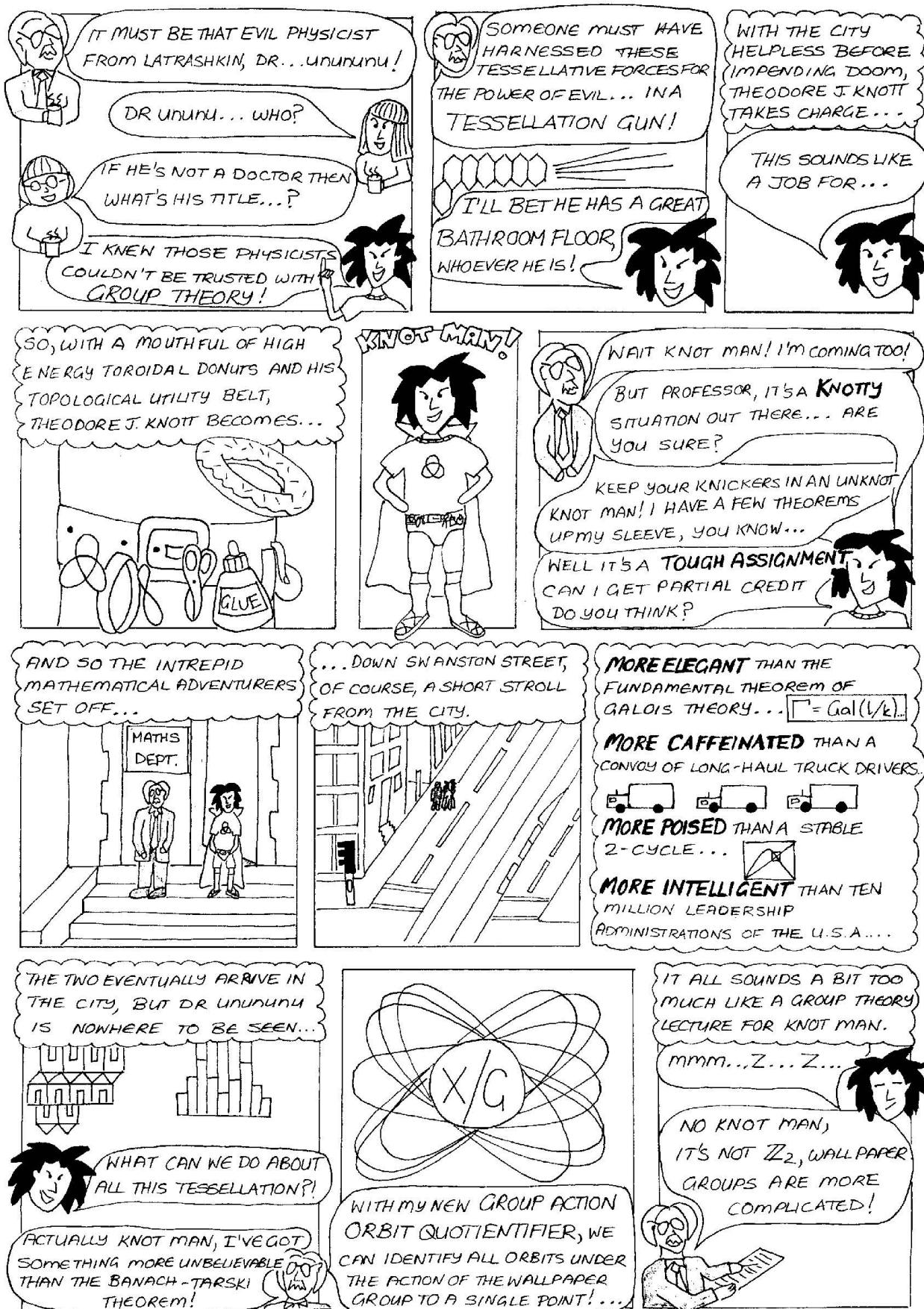
FEEL THE e^x , BE THE e^x , THEODORE J.-SAN!











SURE ENOUGH THE PROFESSOR SOON DISCOVERS THE CORRECT GROUP, AND THE GROUP ACTION ORBIT QUOTIENTIFIER DOES THE REST!

THE CITY IS RETURNED TO NORMAL... WELL ALMOST...

FASTER THAN A QUANTUM COMPUTER, DR UNUNUNU HEADS FOR THE MATHS DEPARTMENT.

BOOHAHAHA... WITH THE MATHEMATICIANS TESSELLATED, I WILL HAVE MORE POWER THAN A TAYLOR SERIES!

CAN'T FIX FEDERATION SQUARE OR RMIT... TOO APERIODIC

QUICK PROFESSOR! IT'S UNUNUNU-HE'S GETTING AWAY!

KNOTMAN AND THE PROFESSOR TAKE THE EMERGENCY TELEPORTER BACK TO THE UNIVERSITY... AND PEOPLE THINK THESE ARE JUST EMERGENCY TELEPHONES!

LOOK OUT!

TAKE THIS, PROF!

PROFESSOR LICKORISH PERFORMS HIS WORLD FAMOUS **LICKORISH TWIST** AND DODGES THE RAY...

YOU KNOW, I HAVE A THEOREM ABOUT THIS!

UNUNUNU'S BARRAGE IS RELENTLESS...

WE'VE GOT TO FIND OURSELVES SOME **COVERING SPACE**, PROF!

YES, HIT THE **DECK TRANSFORMATION** ON THE DOUBLE, KNOT MAN!

REFUGE IS FOUND IN A LITTLE KNOWN NOOK OF THE DEPARTMENT FILLED WITH MATHEMATICAL JUNK...

LUCKY THERE'S A COFFEE MACHINE HERE, EH PROF?

YES, AMAZING FOR SUCH A COMPACT SPACE!

LET'S HAVE A LOOK THROUGH ALL THIS STUFF...
...Hmm...

CONIC SECTIONS... COFACTOR MATRICES...
...ENW... [scribble]

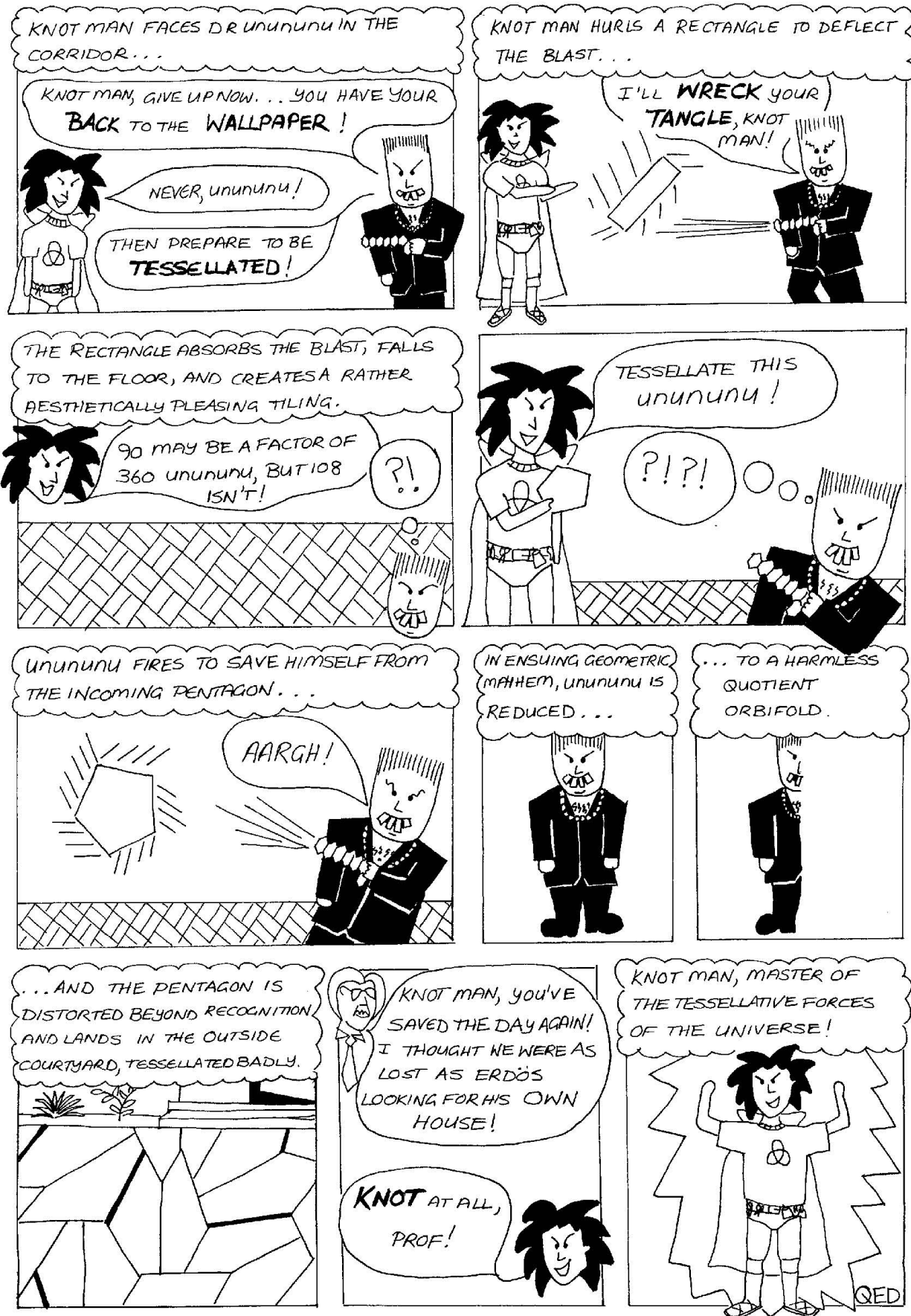
SEVENTY FAILED PROOFS OF THE POINCARÉ CONJECTURE...
[scribble] $\pi_1(x) = 0$

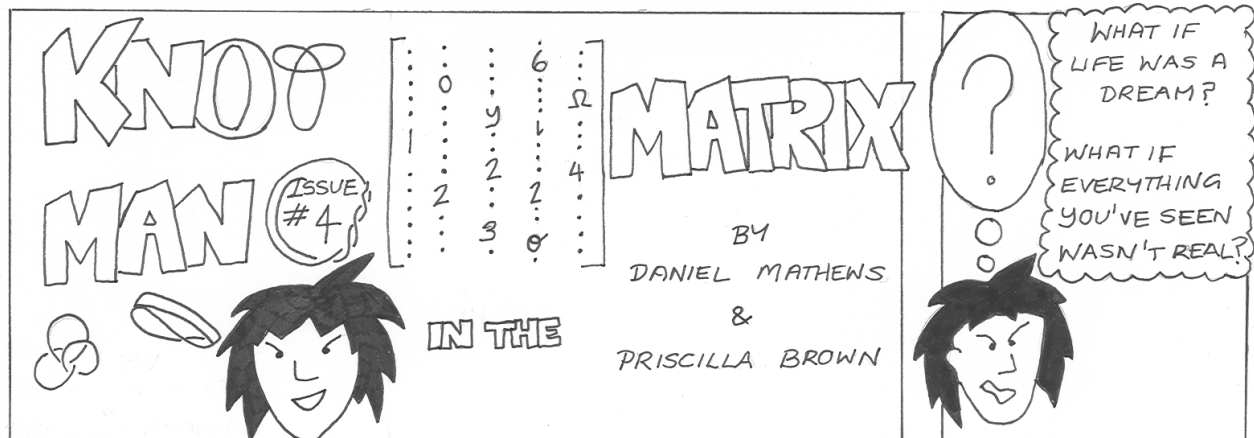
THAT COOL ELECTRON THING THEY BRING OUT EVERY DISCOVERY DAY...

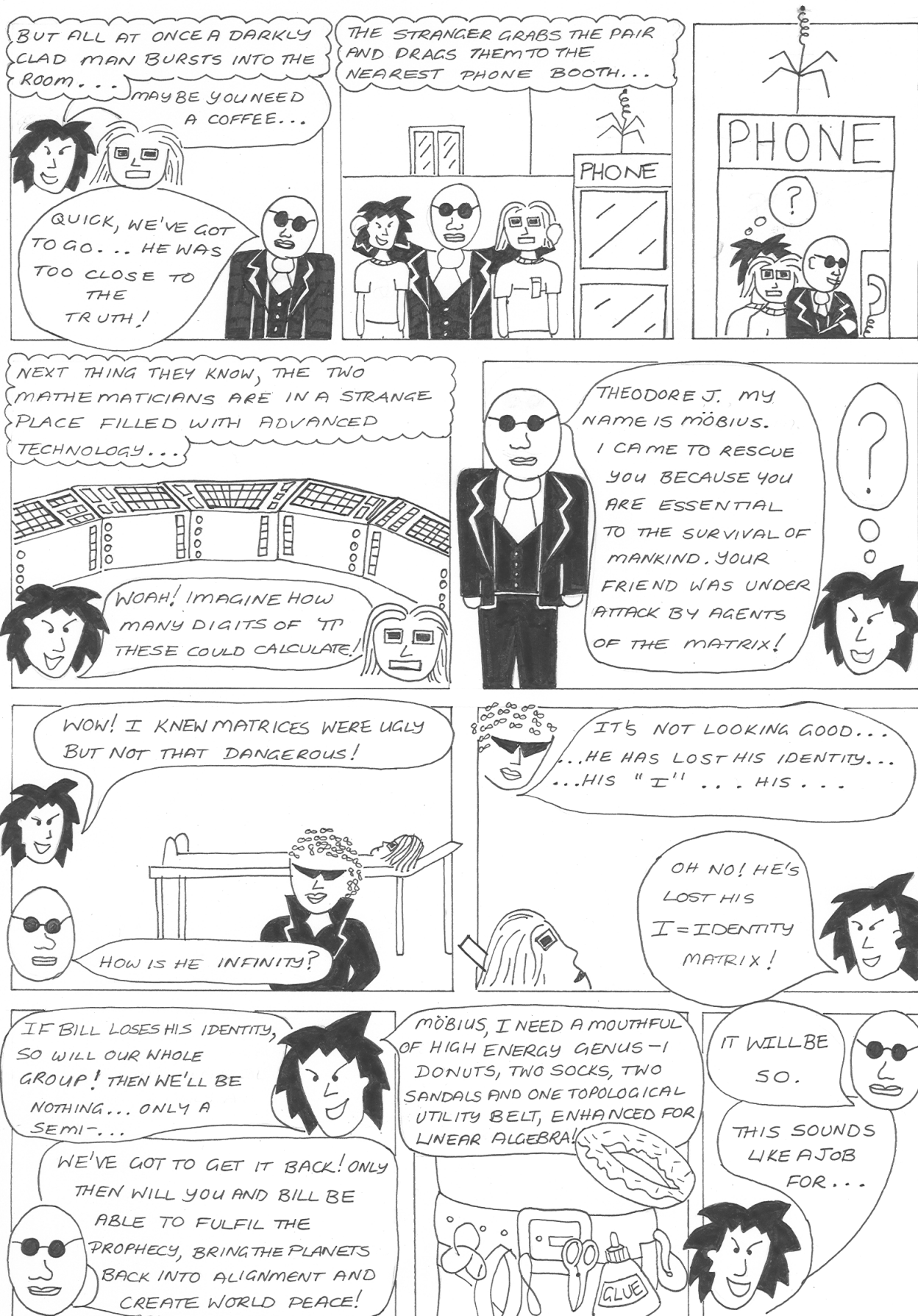
THINGS ARE LOOKING AS HOPELESS AS THE GOLDBACH CONJECTURE WHEN KNOT MAN STUMBLES ON SOMETHING...

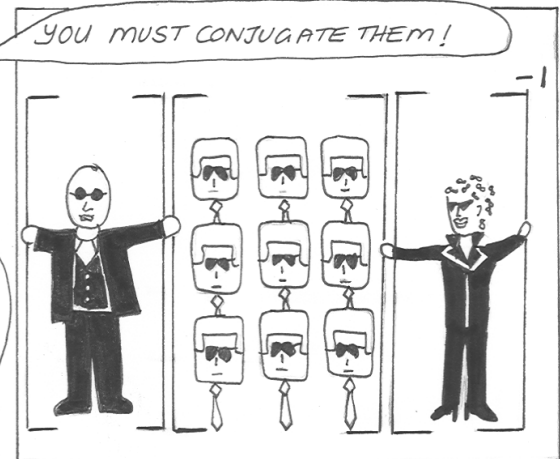
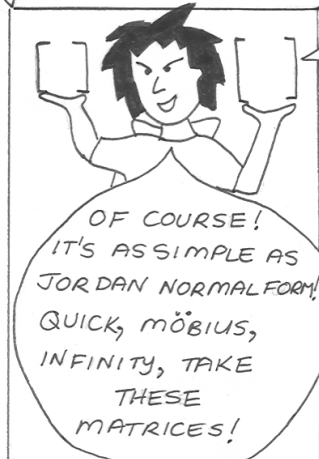
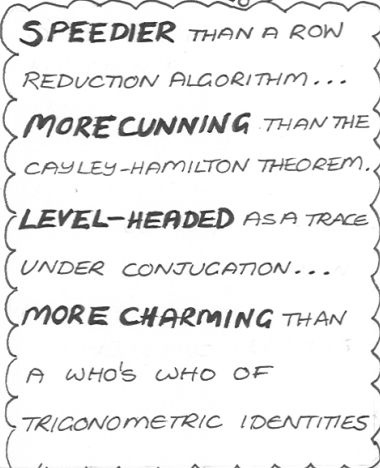
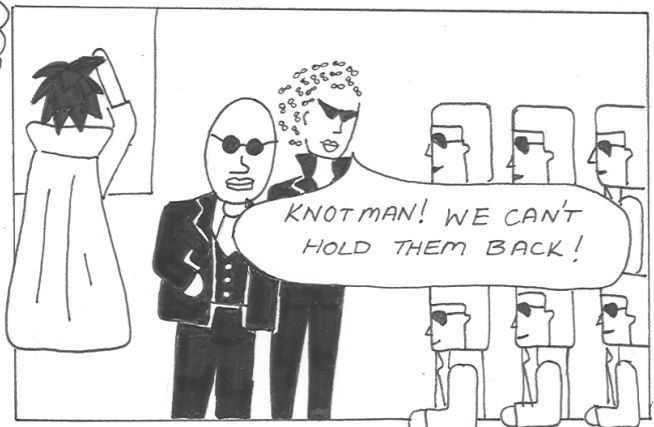
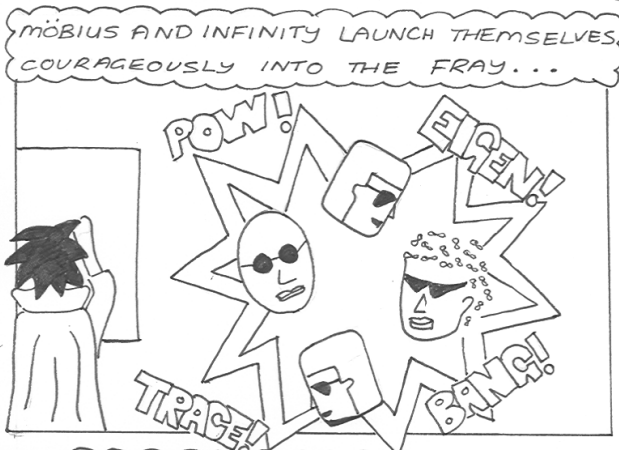
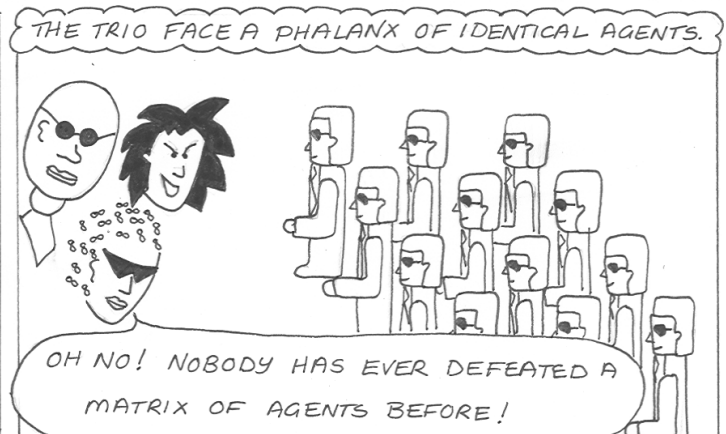
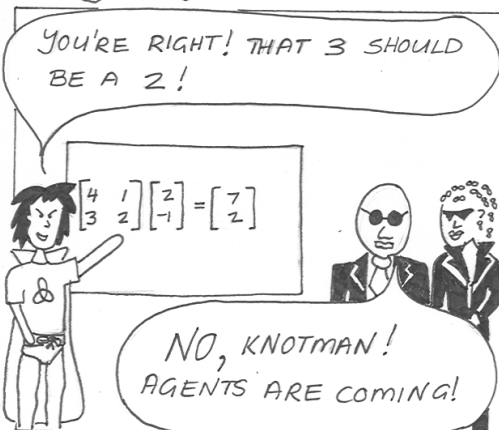
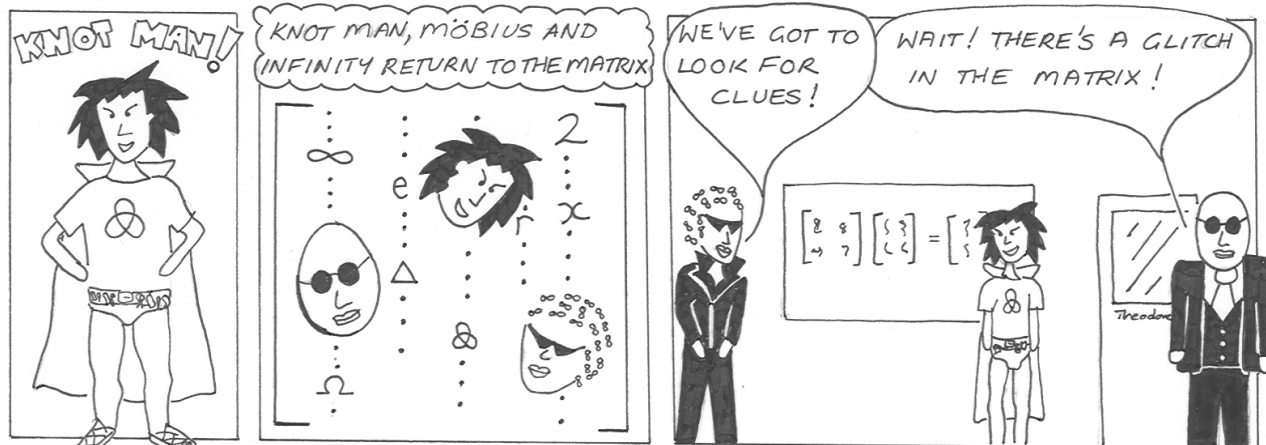
AHA! POLYGONS! NOW I'M READY TO TAKE ON UNUNUNU!

GOOD LUCK KNOT MAN, AND MAY THE TESSELLATIVE FORCES OF THE UNIVERSE BE WITH YOU!











$$\text{Re}(\text{☺}) = \text{◯}$$

$$\text{Im}(\text{☺}) = \text{⋯}$$

$$\nabla \times (\text{☺}) = \text{☺ with curly hair}$$

$$\nabla(\text{☺}) = \text{☺ wearing a graduation cap}$$

$$\int \text{☺}^{-1} d\text{☺} = \text{☺ with a long flame coming out of its mouth}$$

$$\text{sup}(\text{☺}) = \text{☺ in a bowl with steam rising from it}$$

$$\text{sin}(\text{☺}) = \text{☺ on a seesaw}$$

$$\partial(\text{☺}) = \text{☹}$$

$$\text{☺}^{-1} = \text{☹}$$

$$\text{☺}^2 = \text{☺ inside a square}$$

$$\text{☺}^3 = \text{☺ inside a cube}$$